

SOME RESULTS ON $S_{\alpha,\beta}$ AND $T_{\alpha,\beta}$ INTUITIONISTIC FUZZY MODAL OPERATORS

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ABSTRACT. In 1999, first Intuitionistic Fuzzy Modal Operators introduced in[2]. Expansion of these operators and new operators defined by different authors[3, 5, 6, 7, 8, 9]. Characteristics of these operators has been studied by several researchers.

In this study, we obtained new results on modal operators which are called $S_{\alpha,\beta}$ and $T_{\alpha,\beta}$.

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1. INTRODUCTION

The concept of Intuitionistic fuzzy sets was introduced by Atanassov in 1986 [1], form an extension of fuzzy sets[10] by expanding the truth value set to the lattice $[0, 1] \times [0, 1]$.

Intuitionistic fuzzy modal operators defined firstly by Atanassov[1, 2]. Then several extensions of these operators introduced by different authors[2, 8, 5, 6]. Some algebraic and characteristic properties of these operators were studied by several authors.

Definition 1.1. [1] An intuitionistic fuzzy set (shortly IFS) on a set X is an object of the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$$

where $\mu_A(x), (\mu_A : X \rightarrow [0, 1])$ is called the “degree of membership of x in A ”, $\nu_A(x), (\nu_A : X \rightarrow [0, 1])$ is called the “degree of non- membership of x in A ”, and where μ_A and ν_A satisfy the following condition:

$$\mu_A(x) + \nu_A(x) \leq 1, \text{ for all } x \in X.$$

The class of intuitionistic fuzzy sets on X is denoted by $IFS(X)$.

The hesitation degree of x is defined by $\pi_A(x) = 1 - \mu_A(x) - \nu_A(x)$

Definition 1.2. [1] An IFS A is said to be contained in an IFS B (notation $A \sqsubseteq B$) if and only if, for all $x \in X : \mu_A(x) \leq \mu_B(x)$ and $\nu_A(x) \geq \nu_B(x)$.

It is clear that $A = B$ if and only if $A \sqsubseteq B$ and $B \sqsubseteq A$.

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Definition 1.3. [1] Let $A \in IFS$ and let $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\}$ then the above set is called the complement of A

$$A^c = \{\langle x, \nu_A(x), \mu_A(x) \rangle : x \in X\}$$

The intersection and the union of two IFSs A and B on X is defined by

$$A \sqcap B = \{\langle x, \mu_A(x) \wedge \mu_B(x), \nu_A(x) \vee \nu_B(x) \rangle : x \in X\}$$

$$A \sqcup B = \{\langle x, \mu_A(x) \vee \mu_B(x), \nu_A(x) \wedge \nu_B(x) \rangle : x \in X\}$$

The notion of Second Type Intuitionistic Fuzzy Modal Operators was firstly introduced by Atanassov as following:

Definition 1.4. [1] Let X be universal and $A \in IFS(X)$ then

$$(1) \square(A) = \{\langle x, \mu_A(x), 1 - \mu_A(x) \rangle : x \in X\}$$

$$(2) \diamond(A) = \{\langle x, 1 - \nu_A(x), \nu_A(x) \rangle : x \in X\}$$

Definition 1.5. [2] Let X be universal and $A \in IFS(X)$, $\alpha \in [0, 1]$ then

$$D_\alpha(A) = \{\langle x, \mu_A(x) + \alpha\pi_A(x), \nu_A(x) + (1 - \alpha)\pi_A(x) \rangle : x \in X\}$$

Definition 1.6. [2] Let X be universal and $A \in IFS(X)$, $\alpha, \beta \in [0, 1]$ and $\alpha + \beta \leq 1$ then

$$F_{\alpha, \beta}(A) = \{\langle x, \mu_A(x) + \alpha\pi_A(x), \nu_A(x) + \beta\pi_A(x) \rangle : x \in X\}$$

Definition 1.7. [2] Let X be universal and $A \in IFS(X)$, $\alpha, \beta \in [0, 1]$ then

$$G_{\alpha, \beta}(A) = \{\langle x, \alpha\mu_A(x), \beta\nu_A(x) \rangle : x \in X\}$$

Definition 1.8. [2] Let X be universal and $A \in IFS(X)$, $\alpha, \beta \in [0, 1]$ then

$$(1) H_{\alpha, \beta}(A) = \{\langle x, \alpha\mu_A(x), \nu_A(x) + \beta\pi_A(x) \rangle : x \in X\}$$

$$(2) H_{\alpha, \beta}^*(A) = \{\langle x, \alpha\mu_A(x), \nu_A(x) + \beta(1 - \alpha\mu_A(x) - \nu_A(x)) \rangle : x \in X\}$$

$$(3) J_{\alpha, \beta}(A) = \{\langle x, \mu_A(x) + \alpha\pi_A(x), \beta\nu_A(x) \rangle : x \in X\}$$

$$(4) J_{\alpha, \beta}^*(A) = \{\langle x, \mu_A(x) + \alpha(1 - \mu_A(x) - \beta\nu_A(x)), \beta\nu_A(x) \rangle : x \in X\}$$

The simplest One Type Intuitionistic Fuzzy Modal Operators defined in 1999.

Definition 1.9. [2] Let X be a set and $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\} \in IFS(X)$, $\alpha, \beta \in [0, 1]$.

$$(1) \boxplus A = \left\{ \left\langle x, \frac{\mu_A(x)}{2}, \frac{\nu_A(x)+1}{2} \right\rangle : x \in X \right\}$$

$$(2) \boxtimes A = \left\{ \left\langle x, \frac{\mu_A(x)+1}{2}, \frac{\nu_A(x)}{2} \right\rangle : x \in X \right\}$$

After this definition, in 2001, the extension of these operators were defined as following:

Definition 1.10. [3] Let X be a set and $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\} \in IFS(X)$, $\alpha, \beta \in [0, 1]$.

$$(1) \boxplus_\alpha A = \{\langle x, \alpha\mu_A(x), \alpha\nu_A(x) + 1 - \alpha \rangle : x \in X\}$$

$$(2) \boxtimes_\alpha A = \{\langle x, \alpha\mu_A(x) + 1 - \alpha, \alpha\nu_A(x) \rangle : x \in X\}$$

The operators \boxplus_α and \boxtimes_α are the extensions of the operators \boxplus , \boxtimes , resp.

In 2004, Dencheva introduced the second extension of \boxplus_α and \boxtimes_α .

Definition 1.11. [8] Let X be a set and $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\} \in IFS(X)$, $\alpha, \beta \in [0, 1]$.

- (1) $\boxplus_{\alpha,\beta}A = \{\langle x, \alpha\mu_A(x), \alpha\nu_A(x) + \beta \rangle : x \in X\}$ where $\alpha + \beta \in [0, 1]$.
- (2) $\boxtimes_{\alpha,\beta}A = \{\langle x, \alpha\mu_A(x) + \beta, \alpha\nu_A(x) \rangle : x \in X\}$ where $\alpha + \beta \in [0, 1]$.

In 2006, the third extension of the above operators was studied by author . He defined the following operators;

Definition 1.12. [3]Let X be a set and $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\} \in IFS(X)$.

- (1) $\boxplus_{\alpha,\beta,\gamma}(A) = \{\langle x, \alpha\mu_A(x), \beta\nu_A(x) + \gamma \rangle : x \in X\}$
where $\alpha, \beta, \gamma \in [0, 1], \max\{\alpha, \beta\} + \gamma \leq 1$.
- (2) $\boxtimes_{\alpha,\beta,\gamma}(A) = \{\langle x, \alpha\mu_A(x) + \gamma, \beta\nu_A(x) \rangle : x \in X\}$
where $\alpha, \beta, \gamma \in [0, 1], \max\{\alpha, \beta\} + \gamma \leq 1$.

In 2007, author[5] defined a new operator named $E_{\alpha,\beta}$ and studied some of its properties. This operator as following:

Definition 1.13. [5]Let X be a set and $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\} \in IFS(X)$, $\alpha, \beta \in [0, 1]$. We define the following operator:

$$E_{\alpha,\beta}(A) = \{\langle x, \beta(\alpha\mu_A(x) + 1 - \alpha), \alpha(\beta\nu_A(x) + 1 - \beta) \rangle : x \in X\}$$

At the same year, Atanassov introduced the operator $\boxminus_{\alpha,\beta,\gamma,\delta}$ which is a natural extension of all these operators in [3].

Definition 1.14. [3]Let X be a set, $A \in IFS(X)$, $\alpha, \beta, \gamma, \delta \in [0, 1]$ such that

$$\max(\alpha, \beta) + \gamma + \delta \leq 1$$

then the operator $\boxminus_{\alpha,\beta,\gamma,\delta}$ defined by

$$\boxminus_{\alpha,\beta,\gamma,\delta}(A) = \{\langle x, \alpha\mu_A(x) + \gamma, \beta\nu_A(x) + \delta \rangle : x \in X\}$$

In 2008, most general operator $\odot_{\alpha,\beta,\gamma,\delta,\varepsilon,\zeta}$ defined as following:

Definition 1.15. [3]Let X be a set, $A \in IFS(X)$, $\alpha, \beta, \gamma, \delta, \varepsilon, \zeta \in [0, 1]$ such that

$$\max(\alpha - \zeta, \beta - \varepsilon) + \gamma + \delta \leq 1$$

and

$$\min(\alpha - \zeta, \beta - \varepsilon) + \gamma + \delta \geq 0$$

then the operator $\odot_{\alpha,\beta,\gamma,\delta,\varepsilon,\zeta}$ defined by

$$\odot_{\alpha,\beta,\gamma,\delta,\varepsilon,\zeta}(A) = \{\langle x, \alpha\mu_A(x) - \varepsilon\nu_A(x) + \gamma, \beta\nu_A(x) - \zeta\mu_A(x) + \delta \rangle : x \in X\}$$

In 2010, Çuvalcıođlu[6] defined a new operator which is a generalization of $E_{\alpha,\beta}$.

Definition 1.16. [6]Let X be a set and $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\} \in IFS(X)$, $\alpha, \beta, \omega \in [0, 1]$ then

$$Z_{\alpha,\beta}^{\omega}(A) = \{\langle x, \beta(\alpha\mu_A(x) + \omega - \omega.\alpha), \alpha(\beta\nu_A(x) + \omega - \omega.\beta) \rangle : x \in X\}$$

Definition 1.17. [6]Let X be a set and $A = \{\langle x, \mu_A(x), \nu_A(x) \rangle : x \in X\} \in IFS(X)$, $\alpha, \beta, \omega, \theta \in [0, 1]$ then

$$Z_{\alpha,\beta}^{\omega,\theta}(A) = \{\langle x, \beta(\alpha\mu_A(x) + \omega - \omega.\alpha), \alpha(\beta\nu_A(x) + \theta - \theta.\beta) \rangle : x \in X\}$$

The operator $Z_{\alpha,\beta}^{\omega,\theta}$ is a generalization of $Z_{\alpha,\beta}^{\omega}$, and also, $E_{\alpha,\beta}, \boxplus_{\alpha,\beta}, \boxtimes_{\alpha,\beta}$.

Uni-type intuitionistic fuzzy modal operators introduced by author as following;

Definition 1.18. [7]Let X be a universal, $A \in IFS(X)$ and $\alpha, \beta, \omega \in [0, 1]$ then

- (1) $\boxplus_{\alpha,\beta}^{\omega}(A) = \{ \langle x, \beta(\mu_A(x) + (1 - \alpha)\nu_A(x)), \alpha(\beta\nu_A(x) + \omega - \omega\beta) \rangle : x \in X \}$
- (2) $\boxtimes_{\alpha,\beta}^{\omega}(A) = \{ \langle x, \beta(\alpha\mu_A(x) + \omega - \omega\alpha), \alpha((1 - \beta)\mu_A(x) + \nu_A(x)) \rangle : x \in X \}$

Definition 1.19. [7] Let X be a set and $A \in IFS(X)$, $\alpha, \beta, \omega, \theta \in [0, 1]$ then

$$E_{\alpha,\beta}^{\omega,\theta}(A) = \left\{ \left\langle \begin{array}{l} x, \beta((1 - (1 - \alpha)(1 - \theta))\mu_A(x) + (1 - \alpha)\theta\nu_A(x) + (1 - \alpha)(1 - \theta)\omega), \\ \alpha((1 - \beta)\theta\mu_A(x) + (1 - (1 - \beta)(1 - \theta))\nu_A(x) + (1 - \beta)(1 - \theta)\omega) \end{array} \right\rangle : x \in X \right\}$$

Definition 1.20. [7] Let X be a set, $A \in IFS(X)$ and $\alpha, \beta \in [0, 1]$ then

- (1) $B_{\alpha,\beta}(A) = \{ \langle x, \beta(\mu_A(x) + (1 - \alpha)\nu_A(x)), \alpha((1 - \beta)\mu_A(x) + \nu_A(x)) \rangle : x \in X \}$
- (2) $\boxminus_{\alpha,\beta}(A) = \{ \langle x, \beta(\mu_A(x) + (1 - \beta)\nu_A(x)), \alpha((1 - \alpha)\mu_A(x) + \nu_A(x)) \rangle : x \in X \}$

In 2014, new one type intuitionistic fuzzy modal operators were defined in [9].

Definition 1.21. [9] Let X be a set and $A \in IFS(X)$, $\alpha, \beta, \omega \in [0, 1]$ and $\alpha + \beta \leq 1$

- (1) $L_{\alpha,\beta}^{\omega}(A) = \{ \langle x, \alpha\mu_A(x) + \omega(1 - \alpha), \alpha(1 - \beta)\nu_A(x) + \alpha\beta(1 - \omega) \rangle : x \in X \}$
- (2) $K_{\alpha,\beta}^{\omega}(A) = \{ \langle x, \alpha(1 - \beta)\mu_A(x) + \alpha\beta(1 - \omega), \alpha\nu_A(x) + \omega(1 - \alpha) \rangle : x \in X \}$

As above, we get the following diagram;

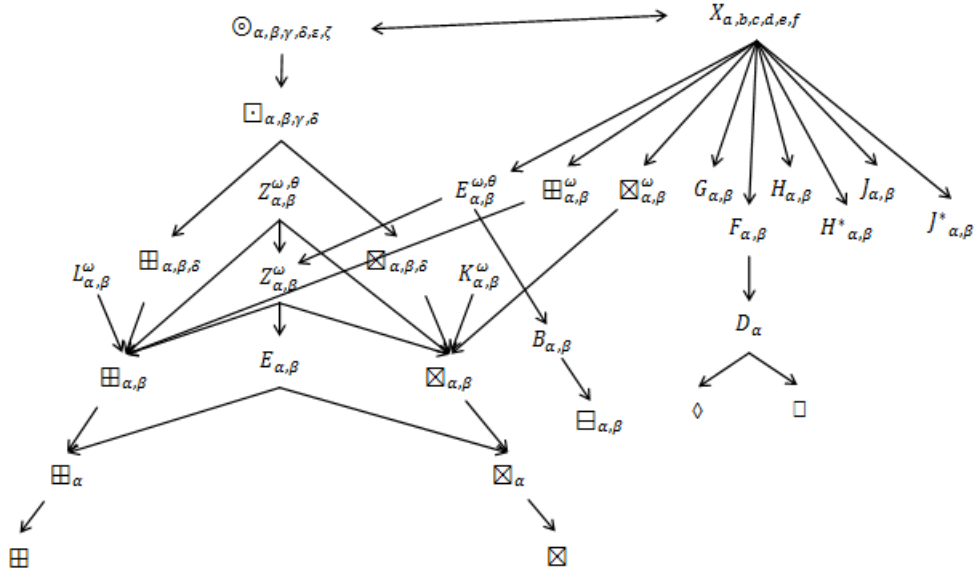


FIGURE 1

The intuitionistic fuzzy modal operator, represented by $\otimes_{\alpha,\beta,\gamma,\delta}$, introduced in 2014 as following;

Definition 1.22. [4] Let X be a set and $A \in IFS(X)$, $\alpha, \beta, \gamma, \delta \in [0, 1]$ and $\alpha + \beta \leq 1, \gamma + \delta \leq 1$ then

$$\otimes_{\alpha,\beta,\gamma,\delta}(A) = \{ \langle x, \alpha\mu_A(x) + \gamma\nu_A(x), \beta\mu_A(x) + \delta\nu_A(x) \rangle \}$$

2. SOME PROPERTIES OF NEW INTUITIONISTIC FUZZY MODAL OPERATORS

Definition 2.1. Let X be a set and $A \in IFS(X)$, $\alpha, \beta, \alpha + \beta \in [0, 1]$.

- (1) $T_{\alpha,\beta}(A) = \{ \langle x, \beta(\mu_A(x) + (1 - \alpha)\nu_A(x) + \alpha), \alpha(\nu_A(x) + (1 - \beta)\mu_A(x)) \rangle : x \in X \}$ where $\alpha + \beta \in [0, 1]$.
- (2) $S_{\alpha,\beta}(A) = \{ \langle x, \alpha(\mu_A(x) + (1 - \beta)\nu_A(x)), \beta(\nu_A(x) + (1 - \alpha)\mu_A(x) + \alpha) \rangle : x \in X \}$ where $\alpha + \beta \in [0, 1]$.

It is clear that;

$$\begin{aligned} \beta(\mu_A(x) + (1 - \alpha)\nu_A(x) + \alpha) + \alpha(\nu_A(x) + (1 - \beta)\mu_A(x)) &= (\mu_A(x) + \nu_A(x))(\alpha + \beta - \alpha\beta) + \alpha\beta \\ &\leq \alpha + \beta - \alpha\beta + \alpha\beta \leq 1 \end{aligned}$$

Theorem 2.1. Let X be a set and $A \in IFS(X)$. If $\alpha, \beta, \alpha + \beta \in [0, 1]$ then $T_{\alpha,\beta}(A)^c = S_{\alpha,\beta}(A^c)$.

Proof. It is clear from definition. □

Proposition 2.1. Let X be a set and $A \in IFS(X)$. If $\alpha, \beta, \alpha + \beta \in [0, 1]$ then

- (1) $T_{\beta,\alpha}(A)^c \sqsubseteq T_{\alpha,\beta}(A^c)$

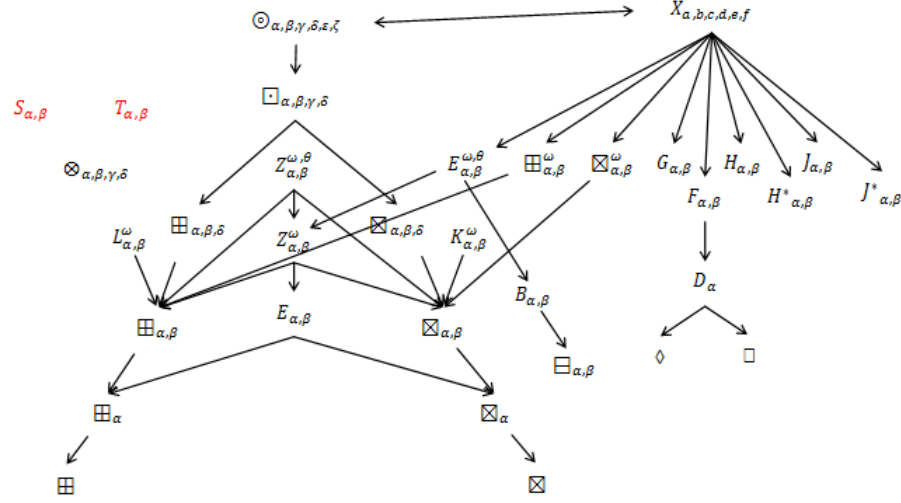


FIGURE 2

$$(2) S_{\alpha,\beta}(A^c) \sqsubseteq S_{\beta,\alpha}(A)^c$$

Proof. (1) From definition of this operators and complement of an intuitionistic fuzzy set we get that,

$$\beta(\nu_A(x) + (1 - \alpha)\mu_A(x)) \leq \beta(\nu_A(x) + (1 - \alpha)\mu_A(x) + \alpha)$$

and

$$\alpha(\mu_A(x) + (1 - \beta)\nu_A(x) + \beta) \geq \alpha(\mu_A(x) + (1 - \beta)\nu_A(x))$$

So, we can say $T_{\beta,\alpha}(A)^c \sqsubseteq T_{\alpha,\beta}(A^c)$.

(2) We can show this inclusion same way. □

Theorem 2.2. Let X be a set and $A \in IFS(X)$. If $\alpha, \beta, \alpha + \beta \in [0, 1]$ and $\beta \leq \alpha$ then

- (1) $T_{\alpha,\beta}(A) \sqsubseteq T_{\beta,\alpha}(A)$
- (2) $S_{\beta,\alpha}(A) \sqsubseteq S_{\alpha,\beta}(A)$

Proof. It is clear. □

Theorem 2.3. Let X be a set and $A, B \in IFS(X)$. If $\alpha, \beta, \alpha + \beta \in [0, 1]$ then

- (1) $T_{\alpha,\beta}(A) \sqcap T_{\alpha,\beta}(B) \sqsubseteq T_{\alpha,\beta}(A \sqcap B)$
- (2) $T_{\alpha,\beta}(A \sqcup B) \sqsubseteq T_{\alpha,\beta}(A) \sqcup T_{\alpha,\beta}(B)$

Proof. (1) Let $\alpha, \beta \in [0, 1]$,

$$\begin{aligned} \beta(1 - \alpha) \min(\nu_A(x), \nu_B(x)) &\leq \beta(1 - \alpha) \max(\nu_A(x), \nu_B(x)) \\ &\Rightarrow \beta(\min(\mu_A(x), \mu_B(x)) + (1 - \alpha) \min(\nu_A(x), \nu_B(x)) + \alpha) \\ &\leq \beta(\min(\mu_A(x), \mu_B(x)) + (1 - \alpha) \max(\nu_A(x), \nu_B(x)) + \alpha) \end{aligned}$$

and

$$\begin{aligned} \alpha(1 - \beta) \max(\mu_A(x), \mu_B(x)) &\geq \alpha(1 - \beta) \min(\mu_A(x), \mu_B(x)) \\ &\Rightarrow \alpha (\max(\nu_A(x), \nu_B(x)) + (1 - \beta) \max(\mu_A(x), \mu_B(x))) \\ &\geq \alpha (\max(\nu_A(x), \nu_B(x)) + (1 - \beta) \min(\mu_A(x), \mu_B(x))) \end{aligned}$$

It is appear from here that $T_{\alpha,\beta}(A) \sqcap T_{\alpha,\beta}(B) \sqsubseteq T_{\alpha,\beta}(A \sqcap B)$.

(2) It can be shown easily. \square

Theorem 2.4. *Let X be a set and $A, B \in IFS(X)$. If $\alpha, \beta, \alpha + \beta \in [0, 1]$ then*

- (1) $S_{\alpha,\beta}(A \sqcup B) \sqsubseteq S_{\alpha,\beta}(A) \sqcup S_{\alpha,\beta}(B)$
- (2) $S_{\alpha,\beta}(A) \sqcap S_{\alpha,\beta}(B) \sqsubseteq S_{\alpha,\beta}(A \sqcap B)$

Proof. (1) Let $\alpha, \beta \in [0, 1]$,

$$\begin{aligned} \alpha(1 - \beta) \min(\nu_A(x), \nu_B(x)) &\leq \alpha(1 - \beta) \max(\nu_A(x), \nu_B(x)) \\ &\Rightarrow \alpha (\max(\mu_A(x), \mu_B(x)) + (1 - \beta) \min(\nu_A(x), \nu_B(x))) \\ &\leq \alpha (\max(\mu_A(x), \mu_B(x)) + (1 - \beta) \max(\nu_A(x), \nu_B(x))) \end{aligned}$$

and

$$\begin{aligned} \beta(1 - \alpha) \max(\mu_A(x), \mu_B(x)) &\geq \beta(1 - \alpha) \min(\mu_A(x), \mu_B(x)) \\ &\Rightarrow \beta (\min(\nu_A(x), \nu_B(x)) + (1 - \alpha) \max(\mu_A(x), \mu_B(x)) + \alpha) \\ &\geq \beta (\min(\nu_A(x), \nu_B(x)) + (1 - \alpha) \min(\mu_A(x), \mu_B(x)) + \alpha) \end{aligned}$$

Thus, $S_{\alpha,\beta}(A \sqcup B) \sqsubseteq S_{\alpha,\beta}(A) \sqcup S_{\alpha,\beta}(B)$.

(2) Can be proved similarly. \square

REFERENCES

- [1] Atanassov K.T., Intuitionistic Fuzzy Sets, VII ITKR's Session, Sofia, June (1983).
- [2] Atanassov K.T., Intuitionistic Fuzzy Sets, Physica-Verlag, Heidelberg, NewYork, (1999).
- [3] Atanassov K.T., Studies in Fuzziness and Soft Computing-On Intuitionistic Fuzzy Sets Theory, ISBN 978-3-642-29126-5, Springer Heidelberg, New York, 2012.
- [4] Atanassov K.T., Çuvalcıođlu, G., Atanassova V. K., A new modal operator over intuitionistic fuzzy sets, Notes on IFS, 20(5), 2014, 1-8.
- [5] Çuvalcıođlu, G., On the diagram of One Type Modal Operators on Intuitionistic Fuzzy Sets: Last Expanding with $Z_{\alpha,\beta}^{\omega,\theta}$, Iranian Journal of Fuzzy Systems Vol. 10, No. 1, (2013) pp. 89-106.
- [6] Çuvalcıođlu G., New Tools Based on Intuitionistic Fuzzy Sets and Generalized Nets, ISBN 978-3-319-26301-4, Springer International Publishing Switzerland, 2016, 55-71.
- [7] Çuvalcıođlu G., Yılmaz S. On New Intuitionistic Fuzzy Operators: $S_{\alpha,\beta}$ and $T_{\alpha,\beta}$, KAMERA, 43(2), 2015, 317-327.
- [8] Dencheva K., Extension of intuitionistic fuzzy modal operators \boxplus and \boxtimes , Proc. of the Second Int. IEEE Symp. Intelligent systems, Varna, June 22-24, (2004), Vol. 3, 21-22.
- [9] Yılmaz, S., Bal, A., Extensıon of Intuitionistic Fuzzy Modal Operators Diagram with New Operators, "Notes on IFS", Vol. 20, 2014, Number 5, pp. 26-35.
- [10] Zadeh L.A., Fuzzy Sets, Information and Control, 8, (1965) , p. 338-353.

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